

# Automatic time series forecasting

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## Outline

- 1 Motivation
- 2 Exponential smoothing
- 3 ARIMA modelling
- 4 The forecast package

## Motivation

- 1 Common in manufacturing to have over one thousand product lines that need forecasting at least monthly.
- 2 Forecasts are often required by people who do not know how to fit appropriate time series models.

### Specifications

Automatic forecasting algorithms must

- determine an appropriate time series model
- estimate the parameters
- compute the forecasts with prediction intervals

## Exponential smoothing

### Reference



Makridakis, Wheelwright and Hyndman (1998) *Forecasting: methods and applications*, 3rd ed., Wiley: NY.

- Until recently, there has been no stochastic modelling framework incorporating likelihood calculation, prediction intervals, etc.
- Ord, Koehler & Snyder (JASA, 1997) and Hyndman, Koehler, Snyder and Grose (IJF, 2002) showed that all ES methods (including non-linear methods) are optimal forecasts from innovation state space models.

## Pegels' (1969) taxonomy

Extended by Gardner (IJF 1985), Hyndman et al. (IJF 2002), and Taylor (IJF 2003).

| Trend Component |                         | Seasonal Component |                   |                       |
|-----------------|-------------------------|--------------------|-------------------|-----------------------|
|                 |                         | N<br>(None)        | A<br>(Additive)   | M<br>(Multiplicative) |
| N               | (None)                  | N,N                | N,A               | N,M                   |
| A               | (Additive)              | A,N                | A,A               | A,M                   |
| A <sub>d</sub>  | (Additive damped)       | A <sub>d</sub> ,N  | A <sub>d</sub> ,A | A <sub>d</sub> ,M     |
| M               | (Multiplicative)        | M,N                | M,A               | M,M                   |
| M <sub>d</sub>  | (Multiplicative damped) | M <sub>d</sub> ,N  | M <sub>d</sub> ,A | M <sub>d</sub> ,M     |

General notation



## Automatic forecasting

**From Hyndman et al. (IJF, 2002):**

- Apply each of 30 methods that are appropriate to the data. Optimize parameters and initial values using MLE (or some other criterion).
- Select best method using AIC:

$$\text{AIC} = -2 \log(\text{Likelihood}) + 2p$$

where  $p = \#$  parameters.

- Produce forecasts using best method.
- Obtain prediction intervals using underlying state space model.

**Method performed very well in M3 competition.**

## ARIMA modelling

### Conventional ARIMA forecasting

- calculate forecasts from the best fitting ARIMA model
- Not necessarily the best forecasting ARIMA model.
- Model identification either subjective and complex, or based on information criteria that may not give good forecasts.

## Automatic Algorithm

### Key ideas

- Fit ARIMA model to  $y_1, \dots, y_t$  and forecast  $y_{t+1|t}, \dots, y_{t+h|t}$
- Calculate out-of-sample error  $a_{t,i} = (y_{t+i} - \hat{y}_{t+i|t})$
- Calculate average

$$\text{MSE}_i = \frac{1}{n-h-m+1} \sum_{t=m}^{n-h} a_{t,i}^2 \text{ and } \text{MSE} = \frac{1}{h} \sum_{i=1}^h \text{MSE}_i$$

- Choose model based on smallest  $\text{MSE}_i$  or smallest MSE.

# Automatic Algorithm

## Problem:

- Procedure involves fitting  $(n - m)D$  model where  $D$  is the number of candidate models.
- Using nonlinear optimization is infeasible.

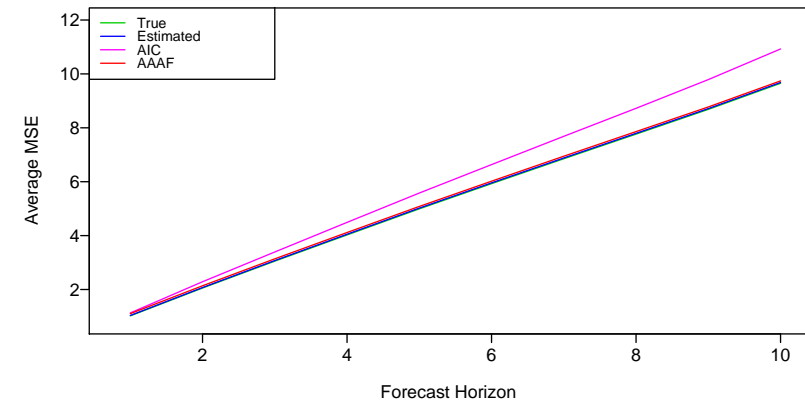
## Solution:

- Estimate error series and fit all models using OLS regression.
- Kalman filter provides very fast updating of coefficients for each model.
- Algorithm involves  $D$  models passed through a Kalman filter.

# Automatic Algorithm

## DGP: ARIMA(0,1,1)

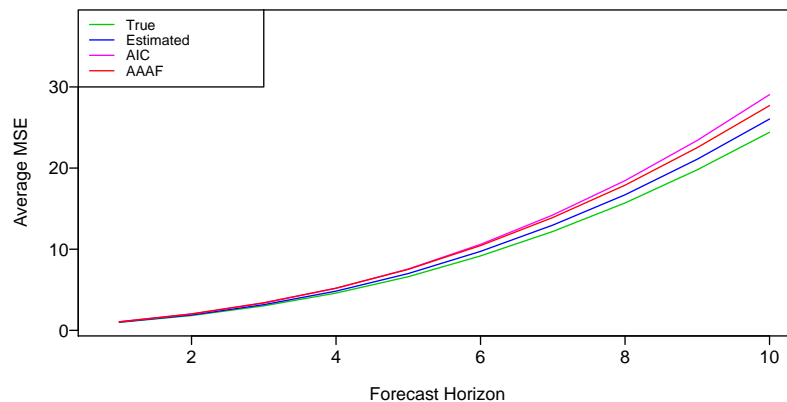
No. of series 1000, with each length 100



# Automatic Algorithm

## DGP: ARIMA(2,1,2)

No. of series 1000, with each length 100



# forecast package

## forecast() function

- Takes a time series as its main argument
- Returns forecasts from automatic ES algorithm.
- Yet to implement automatic ARIMA algorithm.
- Also has methods for objects of arima, HoltWinters and StructTS classes
- Calls predict() when appropriate.
- Output as class "forecast".

## forecast package

### forecast class contains

- Original series
- Point forecasts
- Prediction interval
- Forecasting method used
- Residuals and other information

### Methods applying to the forecast class:

- print
- plot
- summary

## forecast package

> **forecast(beer)**

|          | Point Forecast | Lo 80    | Hi 80    |
|----------|----------------|----------|----------|
| Sep 1995 | 138.2864       | 128.5376 | 148.2387 |
| Oct 1995 | 165.8323       | 154.0843 | 177.8765 |
| Nov 1995 | 182.7895       | 170.0695 | 195.9814 |
| Dec 1995 | 186.1633       | 172.5645 | 199.7450 |
| Jan 1996 | 144.6313       | 133.8904 | 155.3027 |
| Feb 1996 | 137.2431       | 127.2945 | 147.7794 |
| Mar 1996 | 155.1601       | 143.5184 | 166.8024 |
| Apr 1996 | 139.7544       | 129.1742 | 150.2580 |
| ....     |                |          |          |

## forecast package

> **summary(forecast(beer))**

Forecast method: Pegels method MMM

Model Information:

Pegels method MMM

Smoothing parameters:

alpha = 0.05

beta = 0.399

gamma = 0.05

phi = 1

Initial values:

l = 160.5127

b = 0.9965

s = 0.9652 0.9152 1.0322 0.9294 0.9328 0.8479

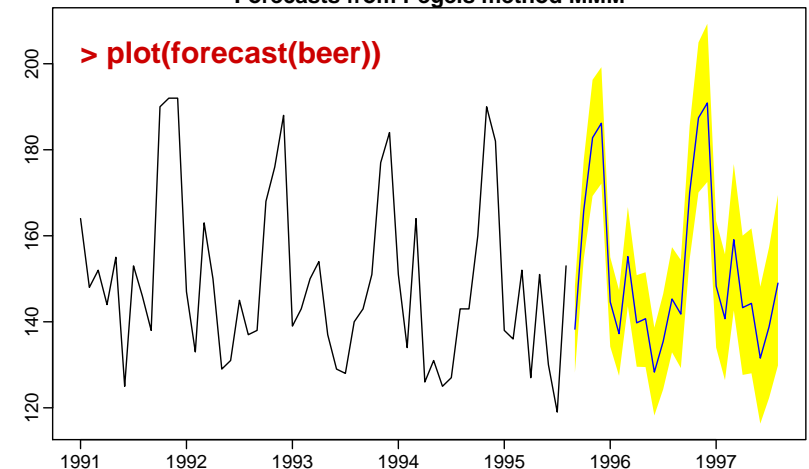
0.8965 0.9565 0.9314 1.1176 1.2275 1.2478

In-sample error measures:

|  | ME          | MSE          | MAE         | MPE         | MAPE        |
|--|-------------|--------------|-------------|-------------|-------------|
|  | 0.693364420 | 65.159550580 | 6.476950267 | 0.001983306 | 0.044197349 |

## forecast package

Forecasts from Pegels method MMM



## forecast package

- Automatic ES forecasting.
- Automatic ARIMA modelling using AIC.
- Forecasting intermittent demand data using Croston's method
- Forecasting using Theta method
- Includes 3003 time series from M3 competition.
- Includes 1001 time series from M competition.
- Includes 90 data sets from Makridakis, Wheelwright & Hyndman (1998)
- Available as compiled Windows binary from <http://www.robhyndman.info/Rlibrary/forecast/>
- Plan to upload to CRAN later this year.